

Magnitude Scales and Their Relations for Taiwan Earthquakes: A Review

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ABSTRACT

The magnitude scales, including M_L , M_D , M_s (GR), m_B , M_s , m_B , M_H , M_J and M_I , applied to quantify earthquakes in the Taiwan region since 1900 are reviewed. Their relations studied by several authors are also discussed.

1. INTRODUCTION

Magnitude is essentially a directly measurable parameter to quantify earthquakes. Since Richter introduced local magnitude in 1935, numerous magnitude scales have been defined and widely used for scientific and practical purpose, for examples, the study on seismicity, the estimation of seismic risk, and earthquake prediction research. The magnitude scales are defined based on different types of seismic waves at different periods of oscillation. Some magnitude scales are not used for the whole time period since 1900. It is necessary to understand the difference and relation between two magnitude scales for establishing a complete earthquake catalogue. Miyamura (1978), Båth (1981), Chung and Bernreuter (1981), and Utsu (1982b) reviewed various magnitude scales and their relations in detail.

Taiwan is a seismologically active region. Historically, a lot of destructive earthquakes shook the region and caused severe damage. Several catalogues, e.g. CMO (1952), Gutenberg and Richter (1954), Duda (1965), Rothé (1969), Hsu (1971, 1980 and 1985), Lee *et al.* (1978), Båth and Duda (1979), Utsu (1979 and 1982a), Abe (1981 and 1984), Abe and Kanamori (1980), Abe and Noguchi (1983a,b), Yeh and Hsu (1985) and Chen and Yeh (1989), include Taiwan earthquakes in different time intervals. A catalog including four volumes for each year has been published by the Central Weather Bureau (CWB, formerly Taiwan Weather Bureau) since 1954. During 1973-1991, a catalog including four volumes for each year was published by the Institute of Earth Sciences, Academia Sinica. Recently, the two catalogues were merged and the new catalog is published by the CWB. In these catalogues, different magnitude scales were used. The relations among the magnitude scales were studied by numerous authors, e.g. Liaw and Tsai (1981), Yeh *et al.* (1982), Wang (1985), Shin (1986), Wang and Chiang (1987), Cheng and Yeh (1989), Li and Chiu (1989), Wang *et al.* (1989, 1990), and Wang and Miyamura (1990).

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In this paper, the magnitude scales used for quantifying Taiwan earthquakes and their relations will be reviewed in detail. The materials are mainly from the papers published in numerous journals. Also included are a few current results done by the author.

2. MAGNITUDE SCALES

(1) Local Magnitude

Richter (1935) defined the local magnitude M_L based on the amplitudes recorded on the Wood-Anderson torsion seismographs with natural period of 0.8 sec, damping factor of 0.8 and magnification of 2800. Richter defined the earthquake, for which the maximum trace amplitude at a distance of 100 km is 1 mm, to be the zero-magnitude earthquake. If $A_o(\Delta)$ expresses the function of the maximum trace amplitude A_o of the zero-magnitude earthquake in terms of epicentral distance Δ , then M_L is given by:

$$M_L = \log A(\Delta) - \log A_o(\Delta) \quad (1)$$

where A is the maximum trace amplitude on the Wood-Anderson seismograph for the earthquake at a distance Δ . A table of $-\log A_o$ as a function of distance Δ (in kilometers) can be found in the text by Richter (1958). Eq. (1) was originally determined only for the southern California earthquakes and for the maximum trace amplitudes with periods of between 0.0 and 0.5 sec, for which the magnification is 2800 for the Wood-Anderson seismograph. The attenuation of seismic waves in this period range is mainly caused by the absorptive properties of the upper layer of the earth's crust. Hence, wide variation in the amplitude versus distance relations over the surface of the earth's crust must be remarkable. However, the M_L scale has been widely used in other geological provinces without regional corrections.

In 1980, a Wood-Anderson seismograph with a magnification of 100, manufactured by Geotech Co., USA was operating at the Institute of Earth Sciences (IES), Academia Sinica. Unfortunately, the seismograph was out of service after 1980. Since 1980, a simulated Wood-Anderson seismograph from a L-4C sensor has been installed at the Institute (Liu, 1981; Wang *et al.*, 1989). Liu (1981) measured the maximum amplitudes of six earthquakes recorded by the two seismographs at the same time. The ratios of the two maximum trace amplitudes change from 0.96 to 1.04 with the average of 1.0, thus indicating that the simulated one can work as a real one. Since 1980, the local magnitudes of Taiwan earthquakes with duration magnitude greater than 4 have been routinely determined based on the Richter's $-\log A_o$ values. However, Wang *et al.* (1989) stressed that the site effects from sediments beneath the station would amplify the short-period signal, thus inflating the M_L value.

From the maximum amplitudes of the displacement seismograms synthesized from the strong-motion accelerograms of 10 events through the technique developed by Kanamori and Jennings (1978), Yeh *et al.* (1982) obtained an amplitude-distance curve for 0-100 km. Due to small number of data points for epicentral distance greater than 50 km, the deviation of their curve from Richter's increases as the epicentral distance increases. Their amplitude-distance relation is used only by Yeh and his coauthors to establish their catalogues and not used in the routine work to determine local magnitude.

(2) Duration Magnitude

Duration magnitude is a different magnitude estimated from the signal duration (F-P) in seconds by using an empirical formula in the general form:

$$M = a_1 + a_2 \log(F - P) + a_3 \Delta + a_4 h \quad (2)$$

where Δ is the epicentral distance in kilometers, h is the focal depth in kilometers and a_1 - a_4 are empirical constants. This magnitude was applied to quantify Russian earthquakes first by Bisztricsany (1958) from the duration of surface waves and by Solove'v (1965) from the total duration of seismogram. However, they used telemetered seismograms for determining magnitude. Tsumura (1967) determined the duration magnitude from the total duration of oscillation from local earthquakes recorded by Wakayama, Japan microearthquake network. His formulation for determining duration magnitude is still used today in Japan for local earthquakes. Lee *et al.* (1972) determined an empirical formula for estimating the duration magnitude for California earthquakes in the form:

$$M_D = -0.87 + 2.00 \log D + 0.0035 \Delta \quad (3)$$

Lee *et al.* determined this formula by using 351 central California earthquakes having local magnitude. They found that the M_L of an earthquake can be estimated by Eq. (3) to within about ± 0.25 unit.

Since 1973, Eq. (3) has been introduced to determine the duration magnitude of Taiwan earthquakes by the use of seismograms recorded by the TTSN (Wang, 1989). Since 1988, when a new short-period seismographic network was placed in operation by the CWB, this magnitude scale has also been used by this agency to determine the magnitude for Taiwan earthquakes. The signal duration used by Lee *et al.* in Eq. (3) was originally defined from the P arrival to the point in the coda where the largest peak-to-peak amplitude on a Geotech model 6585 film viewer (20X magnification) is less than 1 cm. Hence, it is impossible to compare the duration magnitudes determined from different instruments. In other words, earthquake magnitude determined from the total signal duration must be calibrated for each region. The direct use of the duration magnitude formula by Lee *et al.* to the Taiwan earthquakes is based on the assumption that the geological conditions in California are similar to those in Taiwan. Since the coda waves are caused by the scattering of body waves in the heterogeneous media (Aki, 1969), the coda Q (Q_c) is a significant indication to demonstrate the degree of heterogeneity of the media. The Q_c values for the Taiwan region from Chen *et al.* (1989), southern California from Mayeda *et al.* (1991), and central California from Phillips and Aki (1986) are listed in Table 1. It can be seen that the Q_c values of Taiwan are larger than those of southern California and almost equal to those of central California. Since the formula by Lee *et al.* (1972) was deduced mainly from the earthquakes in central California, the direct use of their formula to determine duration magnitude for Taiwan earth-

Table 1. The coda Q values in the considered time intervals for Taiwan from Chen *et al.* (1989), southern California from Mayeda *et al.* (1991) and for central California from Phillipse and Aki (1986).

Frequency (Hz)	Taiwan	Central California		Southern California	
	t<100s	10s<t<30s	30s<t<100s	20s<t<40s	40s<t<100s
1.5	160	137	175	76	107
3.0	273	153	284	167	245
6.0	465	292	448	295	314
12.0	793	576	602	549	629

quakes seems to be acceptable. According to the magnitude values reported in the Preliminary Determination Epicenters (PDE) by US Geological Survey (USGS), Yiu and Lin (1973) deduced a formula for the duration magnitude for Taiwan earthquakes in the form:

$$M_D(YL) = 0.632588 + 1.667354 \log D + 0.000582 \Delta \quad (4)$$

But they did not clearly mention which magnitude scale listed in the PDE was used. After an examination of their data set, it is found that their calibration magnitude is the body-wave magnitude. Comparison of Eq. (3) with Eq. (4) shows that the epicentral term is less important in the latter than in the former, and actually can be ignored in the practical calculation by using Eq. (4). However, Yiu and Lin's formula has not been applied to determine the duration magnitude for Taiwan earthquakes.

According to the coda wave theory, Shin (1986) studied the station correction of Eq. (3) for the TTSN. His revised formula is in the form:

$$M_D(Shin) = -0.87 + 2.00 \log D + 0.0023 \Delta + R \quad (5)$$

where R is the station correction and its value is in the range of from -0.01 to 0.45. He also related $M_D(Shin)$ to M_D in the form:

$$M_D(Shin) = 0.955 M_D + 0.16 \quad (6)$$

Essentially, there is only small difference between M_D and $M_D(Shin)$

(3) Body-wave and Surface-wave Magnitudes

From the definition of body-wave and surface-wave magnitudes defined by Gutenberg and Richter in a series of papers, the two magnitude scales were very important for earthquake quantification before 1965. Gutenberg (1945a) defined the surface-wave magnitude in the form:

$$M_s(GR) = \log A + 1.656 \log \Delta + 1.818 + C \quad (7)$$

In this formula, A is the vector sum of the maximum amplitudes with period around 20 sec in mm along two horizontal components, Δ is the epicentral distance in degree, and C is the station correction. As only one component amplitude is available, A is the value of the maximum amplitude multiplied by $\sqrt{2}$ or 1.4. However, from empirical test, Lienkaemper (1984) showed 1.2 to be a better estimation of the vector sum than 1.4. This formula is mainly appropriate for epicentral distance in the range of from 15° to 130° . For very large earthquakes, the magnitude might be underestimated through Eq. (7). On the other hand, small earthquakes can not be accurately determined by using Eq. (7) due to limited number of data. Lienkaemper also reported that the two horizontal components of the maximum amplitude were not required to be simultaneous by Gutenberg and the periods of the maximum amplitude did not always lie between 18 to 22 sec, actually as low as 12 sec and as high as 23 sec for some cases.

Gutenberg (1945b,c) also defined a body-wave magnitude to classify shallow and deep earthquakes based on P and S waves in the following form:

$$m_B = \log(A/T) + q(\Delta, h) \quad (8)$$

where T is the period related to the maximum amplitude A and $q(\Delta, h)$ is the correction term associated with epicentral distance (Δ) and focal depth (h). Gutenberg (1945a,b) also provided tabulations for the calculation of this term. The maximum amplitude was selected in several ways: (a) the vertical or composite horizontal component of P phase; (b) the vertical or composite horizontal component of PP phase; and (c) the composite horizontal component of S phase. As only one horizontal component seismogram is available, a value of the maximum amplitude multiplied by $\sqrt{2}$ or 1.4 is taken into account. Before 1950, the intermediate-period instruments were commonly operated, thus the medium-period wave motions were used for the determination of this body-wave magnitude. After careful examination, Abe and Kanamori (1980) stated that in the text of Gutenberg and Richter (1954), for $m_B > 6.9$, the period of P waves used for the determination of magnitude is mainly of from 4 sec to 11 sec with a predominant period of about 7.8 ± 2.3 sec for shallow events, 6.4 ± 1.8 sec for intermediate-depth events and 5.5 ± 1.4 sec for deep events. Gutenberg and Richter (1954) stated that the magnitude for well-observed earthquakes was assigned to the tenth of the unit, with an error less than two tenths, and for the majority of earthquakes, the magnitude was given to the nearest quarter unit. The M_s (GR) and m_B were originally adjusted to coincide near $M=7$, but were later found to be linearly divergent. Several linear relations were deduced for the two magnitudes by Gutenberg and Richter in a series of papers. Finally, Gutenberg and Richter (1956a) related M_s (GR) to m_B in the form:

$$m_B = 0.63M_s(GR) + 2.5 \quad (9)$$

This formula was applied by them to calculate the m_B from M_s (GR) for the earthquakes whose m_B values could not be determined.

From Gutenberg's original note, Abe and Kanamori (1980) found a sign error in the expression for m_B - M_s (GR). They revised this error and deduced a new formula:

$$m_B = 0.57M_s(GR) + 3.0 \quad (10)$$

However, both Eq. (9) and Eq. (10) can not fit the so-called class 'a' data for large earthquakes listed in Geller and Kanamori (1977). But, on the other hand, Gutenberg and Richter (1956a) showed that Eq. (9) fitted the data of m_B vs. M_s (GR) very well. A close examination of Gutenberg and Richter's original data, Abe and Kanamori (1980) stressed that the m_s value (body-wave magnitude calculated from M_s (GR) through Eq. (10)) used in their paper was actually a certain weighted average of m_B and M_s (GR) rather than the real m_s . Lienkaemper (1984) stated that M_{GR} used in the text of Gutenberg and Richter was calculated in a form: $M_{GR} = f_1 M_s(GR) + f_2 m_B$, where $M_B = 1.33(m_B - 1.75)$. For some events, f_1 and f_2 are $2/3$ and $1/3$, respectively. But actually no single weighting between M_s and m_B to compute M_{GR} held for all events. Hence, Eq. (9) as well as Eq. (10) is not a good fit to the data points of m_B vs. M_s (GR). Besides, Abe and Kanamori (1980) also pointed out that the two equations were determined from the data set which consists of events with M_s (GR) in a limited range of from 6 to 7.5. For large events, Abe and Kanamori (1980) deduced a new conversion formula for m_B and M_s (GR) in the form:

$$m_B = 0.65M_s(GR) + 2.5 \quad (11)$$

Abe (1984) stated that M_s (GR) was approximated by $1.25m_B - 1.75$ for deep and intermediate-depth events.

Since the early 1960's, the World-Wide Standard Seismographic Network (WWSSN) has been installed for monitoring the global earthquakes. The body-wave magnitude and surface-wave magnitude have been determined from the maximum trace body-wave amplitude and surface-wave amplitude, respectively in the seismograms recorded by the WWSSN. The surface-wave magnitude is determined by the so-called "Prague-Moscow formula" by Venek *et al.* (1962) and denoted as M_s :

$$M_s = \log(A/T) + 1.66\log\Delta + 3.3 \quad (12)$$

where A is the peak amplitude, T is the period of the peak amplitude and Δ is the epicentral distance in degrees. This formula has been accepted by the International Association of Seismology and Physics of Earth's Interior (IASPEI) since 1966 for the determination of surface-wave magnitude of earthquake. In the practical calculation, only the peak amplitude with period of 20 ± 2 sec is used.

Using the data in Gutenberg and Richter's unpublished research notes, Lienkaemper (1984) recomputed $M_s(L)$ through Eq. (7). Comparison of $M_s(GR)$ and $M_s(L)$ leads to two points: (i) single-station magnitudes in the research notes tend to be larger by 0.1 unit of M_s than $M_s(L)$ and (ii) values of $M_s(GR)$ were larger than simple average of all single-station $M_s(L)$ by 0.16 unit of M_s on average. This 0.16 unit excess of $M_s(GR)$ over $M_s(L)$ is close to 0.18 difference between Eq. (7) and Eq. (12) at $T=20$ sec, i.e., $M_s = \log A + 1.66\log\Delta + 2.0$.

In May, 1968, the United State Coast and Geodetic Survey (USCGS) began publishing in "Earthquake Determination Reports" (EDR) the amplitudes and periods of surface-wave maximum displacements used in the PDE average M_s . In September, 1973, PDE operations were transferred to the USGS. Magnitude was computed, until April 1975, with the Prague-Moscow formula using: (i) vector sum of the horizontal components for those maximums with periods $T=18$ to 22 sec, and (ii) for event shallower than 50 km and epicentral distances of 20° to 160° . Beginning May 1975, PDE averages were based on the maximum vertical instead of horizontal component. Although theoretically the ellipticity of Rayleigh waves would make $M_s(\text{Vertical})$ be greater than $M_s(\text{Horizontal})$, the observed differences are negligible (Hunter, 1972; Abe, 1981). The catalog by Gutenberg and Richter (1954) only includes events which occurred before 1954; while the WWSSN was installed after 1960. Hence, it is impossible to compare $M_s(GR)$ and M_s directly. However, in the Rothe's catalog (1969), $M_s(GR)$ was also used. Abe and Kanamori (1980) compared M_s and $M_s(GR)$ from Rothe's catalog and concluded that $M_s(GR)$ is higher than M_s by about 0.1 on the average. Lienkaemper (1984) stressed that $M_s(GR)$ and M_s of PDE differ only slightly for shallow earthquakes ($h < 40$ km) and one could treat PDE average M_s as directly comparable to M_{GR} with correction. He also mentioned that adding 0.06 to M_s values published in Abe (1981) for events between 1910 to 1952, $h < 40$ km would adjust them to a scale compatible with PDE M_s . Since the installation of the WWSSN in the early 1960's, the body-wave magnitude has been determined almost exclusively from the vertical component of the P wave ground motions at a period of approximately 1 sec through Eq. (8) and represented by m_B . The difference between m_B and m_B has been studied by numerous authors. Guyton (1964) stated that the m_B values for a single earthquake, determined from body waves at different seismographic stations, commonly vary by 0.5 or more, despite corrections for differences in epicentral distance among the stations. This variation, which is related to the differences in amplitudes of a factor of 3 or more, is generally due to azimuthal, instrumental and geological differences among the stations. Romney (1964) and Geller and Kanamori (1977) reported that the m_B values are about 0.3-0.6 units higher than the m_b values. Abe and Kanamori (1980) expressed that m_B is systematically larger than m_b by about 1.3 on the average for events with $m_B > 7$.

For $5.5 < m_B < 7.8$, Abe (1981) stated that m_b is lower than m_B by about 0.4-1.1 units. He also deduced a relation for the two magnitudes in the form:

$$m_B = 1.5m_b - 2.2 \quad (13)$$

(4) Hsu's Magnitude

In order to determine the magnitude for Taiwan earthquakes, Hsu (1971) corrected the surface-wave magnitude, measured from the seismograms recorded by the WWSSN, to the maximum trace amplitude (A) and epicentral distance (Δ) recorded by the displacement-type seismographs of the old network of the CWB. Since the number of earthquakes having M_s value was very small before 1970, he had to calculate the M_s values from the m_B values. However, the conversion formula between the two magnitudes for Taiwan earthquakes was not given at that time. He had to use a M_s - m_b relation:

$$M_s = 0.76m_b + 1.58 \quad (14)$$

obtained by Ichikawa (1966) for Japanese earthquakes for conversion. His formulae for estimating the magnitude actually vary at different stations. But for the practical computation, he suggested an average formula:

$$M_H = \log A + 1.09 \log \Delta + 0.50 \quad (15)$$

It is noted that this relation is applied to determine the M_H values at several stations, and then the average M_H value is calculated from the given M_H values. Hsu used this magnitude scale to quantify Taiwan earthquakes before 1978. The M_s - m_b conversion formula for Japanese earthquakes is different from that for Taiwan earthquakes:

$$M_s = 1.356m_b - 1.736 \quad (16)$$

by Wang (1985). As shown in Figure 1, for $m_b > 5.56$, M_s (Taiwan) is higher than M_s (Japan) and vice versa for $m_b < 5.56$. Hence, the M_H might be overestimated for $m_b < 5.56$ and underestimated for $m_b > 5.56$.

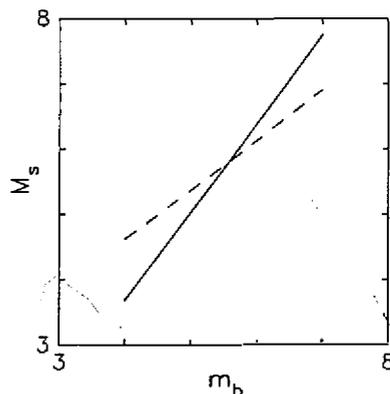


Fig. 1. Figure shows the M_s - m_b relations for Taiwan earthquakes (in solid line) and Japanese earthquakes (in dashed line).

(5) JMA Magnitude

The magnitudes of earthquakes in Japan and some larger earthquakes in Taiwan are routinely determined by the Japanese Meteorological Agency (JMA, formerly Central Meteorological Observatory) by using the formula obtained by Tsuboi (1951):

$$M_J = \log A + 1.731 \log \Delta - 0.83 \quad (17)$$

where A is either the larger value of the maximum amplitudes along two horizontal components or the composite value of the two maximum amplitudes in μm and Δ is the epicentral distance in km. This magnitude was denoted as M_U in Wang and Miyamura (1990) and Wang *et al.* (1990). Hayashi and Abe (1984) reported that the average period of wave motions used for determining M_J is about 3 sec and this magnitude agrees very well with M_s . However, M_J deviates very systematically from M_s as M_s decreases, and M_J is overestimated by as much as 0.6 at $M_s=4$.

(6) Kawasumi's Intensity Magnitude

Kawasumi (1943) defined a magnitude M_I (denoted by M_K in his papers) based on the intensity value at an epicentral distance of 100 km. The intensity scale is the Japanese scale in 8 degrees from 0 to VII, which has been used in Taiwan by combining VI and VII to be VI. The formula for the conversion of intensity of degree I and magnitude M_I as the epicentral distance (Δ) is not equal to 100 km is in the form:

$$I = M_I + 2 \ln(100/\Delta) - 0.00183(\Delta - 100) \quad (18)$$

and

$$I = M_I + 2 \log(r_o/r) - 0.01668(r - r_o) \quad (19)$$

where Δ =epicentral distance; r =hypocentral distance; and r_o =hypocentral distance at $\Delta=100$ km. Late, Kawasumi (1951) related M_I to M_L in the following form:

$$M_L = 4.85 + 0.5M_I \quad (20)$$

Wang *et al.* (1990) expressed that the correlation between M_I with other magnitudes is not good enough. Thus, they proposed that the M_I might be not an appropriate magnitude to quantify Taiwan earthquakes.

(7) Moment Magnitude

The seismic moment $M_o = \mu A u$, where μ is the shear modulus, A is the fault area and u is the spatial average slip on the fault during the earthquake occurrence, was first applied by Aki (1966) to quantify earthquake. The seismic moment can be related to the energy release in earthquakes. Aki (1966, 1967) showed that the amplitude of very long period waves is proportional to M_o and Ben-Menahem *et al.* (1969) also stated that the far-field static-strain field is also proportional to M_o . Besides, because M_o does not saturate, it is a good parameter to represent the size of great earthquakes and has been applied to define moment magnitude by Kanamori (1977) and Hanks and Kanamori (1979). Kanamori (1977)

related the seismic energy (E_s) given by $M_o/(2 \times 10^4)$ to a moment magnitude using the formula by Gutenberg and Richter (1956b):

$$\log E_s = 1.5M_s + 11.8 \quad (21)$$

The moment magnitude (M_w) is defined as

$$M_w = (2/3)\log M_o - 10.7 \quad (22)$$

under an assumption that stress drop is constant. In Eq. (22), M_o is in the unit of dyne-cm. Hanks and Kanamori (1979) stated that Eq. (22) is uniformly valid for $3 < M_L < 7$, $5 < M_s < 7.5$ and $M_w > 7.5$. The M_o values for larger events can be found in the EDR. According to the method proposed by Bolt and Herraiz (1983), Li and Chiu (1989) estimated the seismic moment of Taiwan earthquakes from the simulated Wood-Anderson seismograms. Their resultant formula is in the form:

$$\log M_o(LC) = (16.74 \pm 0.20) + (1.22 \pm 0.14)\log(C \times D \times \Delta) \quad (23)$$

where C is the peak-to-peak amplitude, D is the duration between the S-arrival and the onset of the signal with amplitude of C/d and Δ is the epicentral distance. They stated that the optimum estimation for seismic moment can be obtained as $d=2$.

3. RELATIONS BETWEEN MAGNITUDE SCALES

The relations between magnitudes obtained by numerous authors will be described as follows. It is noted that the data points of m_b - M_H can not be described by a single regression equation due to high dispersion (Wang and Miyamura, 1990), thus will not be discussed further. Basically six groups of relations are discussed.

(1) Relations of M_L vs. M_D , M_L vs. M_H and M_L vs. m_b

Three relations of M_L vs. M_D were studied by three groups of authors. They are

$$M_L = 0.33 + 1.04M_D \pm 0.23 \quad (24)$$

by Liaw and Tsai (1981);

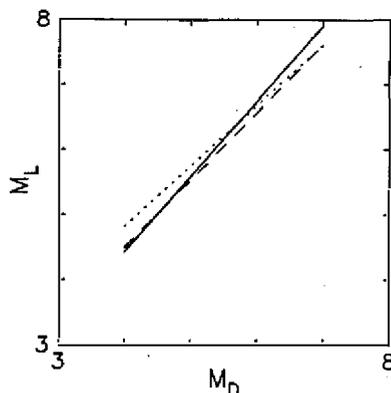
$$M_L(\text{Yeh}) = 1.10 + 0.93M_D \pm 0.30 \quad (25)$$

by Yeh *et al.* (1982); and

$$M_D = (0.187 \pm 0.373) + (0.862 \pm 0.066)M_L \quad (26)$$

by Wang *et al.* (1989). Since M_L determined by Yeh *et al.* (1982) was based on the $-\log A_o$ values obtained by themselves and is denoted by $M_L(\text{Yeh})$. The three equations are plotted in Figure 2. It is obvious that the three equations are close to one another despite the

Fig. 2. Figure shows the M_L - M_D relations from Liaw and Tsai (1981) in dashed line, Yeh *et al.* (1982) in dotted line and Wang *et al.* (1989) in solid line.



use of different data sets to determine the equations. Hsu's catalog in Hsu (1971, 1980, and 1985) contains the most complete instrumentally-determined seismic data during 1900-1978. It is necessary to compare local magnitude M_L , which has been used since 1973, with M_H before the establishment of a complete catalog for Taiwan earthquakes. Yeh *et al.* (1982) first related M_H to their local magnitude M_L (Yeh) in the form:

$$M_L(\text{Yeh}) = 2.63 + 0.56M_H \pm 0.27 \quad (27)$$

A relation between the two magnitudes was determined by Yeh and Hsu (1985) in the following form:

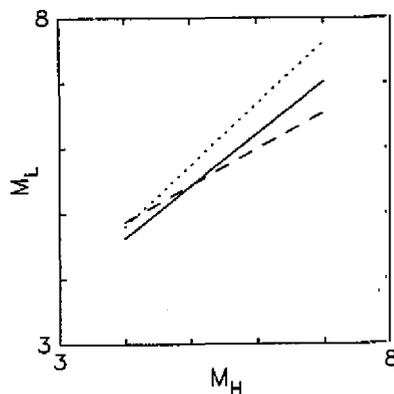
$$M_L(\text{Yeh}) = 1.04 + 0.94M_H \pm 0.28 \quad (28)$$

Cheng and Yeh (1989) obtained a slightly different form for the relation between the two magnitudes:

$$M_L(\text{Yeh}) = 1.42 + 0.80M_H \pm 0.27 \quad (29)$$

The three equations are shown in Figure 3. It is evident that for $M_H > 6$, the M_L values

Fig. 3. Figure shows the M_L - M_H relations from Yeh *et al.* (1982) in dashed line, Yeh and Hsu (1985) in dotted line and Cheng and Yeh (1989) in solid line.



determined from Eq. (28) are larger than those from Eqs. (27) and (29) by 0.5 unit. It is interesting and necessary to compare m_b and M_L . Both of them are determined from the

peak amplitudes of around 1 sec: m_b is according to the telemetered P waves, while M_L is based on the local S waves or Lg waves. Three relations between the two magnitudes have been determined:

$$m_b = 0.27 + 0.85M_L \pm 0.60 \quad (30)$$

by Shin (1986);

$$M_L = (-0.604 \pm 0.485) + (1.268 \pm 0.094)m_b \quad (31)$$

by Wang *et al.* (1989); and

$$M_L = 1.94 + 0.75m_b \quad (32)$$

by Cheng and Yeh (1989). The three regression equations are shown in Figure 4.

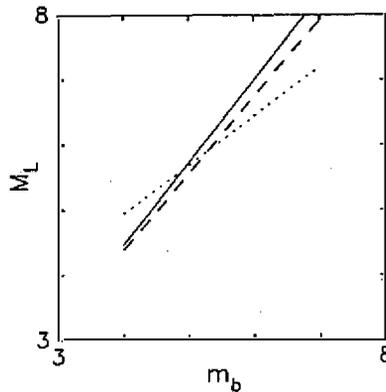


Fig. 4. Figure shows the M_L - m_b relations from Shin (1986) in dashed line, Cheng and Yeh (1989) in dotted line and Wang *et al.* (1989) in solid line.

Essentially, Eqs. (30) and (31) are close to each other, while Eq. (32) remarkably deviates from the other two. For $m_b < 5$, the M_L values from Eq. (32) are smaller than those from Eqs. (30) and (31), but vice versa for $m_b > 5$.

(2) Relations of M_D vs. m_b and M_D vs. M_s

Wang and Chiang (1987) compared M_D with m_b and M_s for shallow earthquakes with focal depth less than 40 km and deep ones with focal larger than 40 km. The data points for M_D vs. m_b are quite dispersive and most events have m_b values in a small range of from 4.8 to 5.5. The M_D - m_b relation for earthquakes with focal depth greater than zero is:

$$M_D = (-1.193 \pm 0.459) + (1.211 \pm 0.097)m_b \quad (33)$$

Although the number of data points of M_D vs. M_s is small, their relation was determined by Wang and Chiang (1987) in the form:

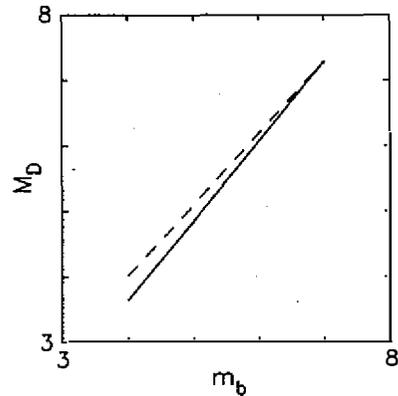
$$M_D = (3.442 \pm 0.632) + (0.374 \pm 0.106)M_s \quad (34)$$

Shin (1986) related m_b to M_D (Shin) in the form:

$$m_b = 0.3 + 0.92M_D(\text{Shin}) \pm 0.5 \quad (35)$$

Eqs. (33) and (35) are similar as shown in Figure 5.

Fig. 5. Figure shows the M_D - m_b relations from Shin (1986) in dashed line and Wang and Chiang (1987) in solid line.



(3) Relations of M_H and other magnitudes

Since the relation between M_H and M_L was given in (1) of this section, only the relations of M_H vs. M_s (GR), M_H vs. M_s , M_H vs. m_b and M_H vs. M_J are presented here. It is noted that the M_H is determined from the seismograms recorded at the local stations, while the other four magnitude scales are determined from the seismograms recorded at the stations outside Taiwan.

The relations of M_s (GR) vs. M_H and M_J vs. M_H given by Wang *et al.* (1990) are:

$$M_s(GR) = (1.12 \pm 0.59) + (0.85 \pm 0.08)M_H \quad (36)$$

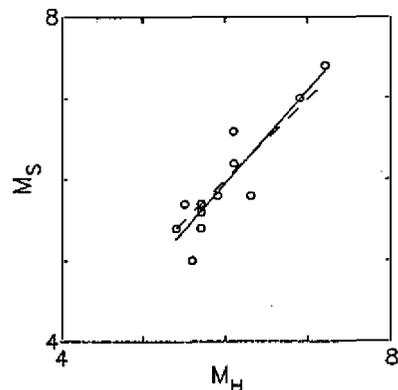
and

$$M_J = (1.26 \pm 0.55) + (0.82 \pm 0.08)M_H \quad (37)$$

The two regression equations are very similar. As the previous mention, the M_H was originally defined based on the surface-wave magnitude M_s . A comparison between the two magnitudes is significant. Figure 6 shows the data points of M_s vs. M_H . The regression equation for the data points is in the form:

$$M_s = (-0.95 \pm 0.31) + (1.15 \pm 0.05)M_H \quad (38)$$

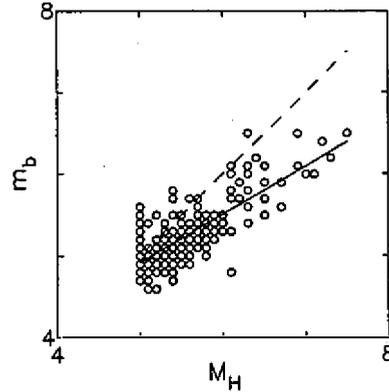
Fig. 6. Figure shows the data points (in open circle) of M_s vs. M_H , the related regression equation (in solid line) and the bisection line (in dashed line).



The bisection line (denoted by dashed line in Figure 6) is very similar to the regression line (in solid line), thus implying the equality of the two magnitudes for Taiwan earthquakes. Although the M_H was determined from local seismic data, it is like the surface-wave magnitude M_s . However, from Eq. (38), as $M_H > 6.3$, $M_H < M_s$ and as $M_H < 6.3$, $M_H > M_s$.

It is also interesting to compare M_H with m_b because the determination of M_H was actually originally from m_b through a conversion formula of M_s and m_b . Figure 7 shows

Fig. 7. Figure shows the data points (in open circle) of m_b vs. M_H , the related regression equation (in solid line) and the bisection line (in dashed line).



the data points of m_b vs. M_H . It is obvious that almost all data points are below the bisection line. The regression equation to fit the data points is in the form:

$$m_b = (1.96 \pm 0.24) + (0.59 \pm 0.00)M_H \quad (39)$$

Although Wang *et al.* (1990) suggested that M_I is not an appropriate magnitude to quantify Taiwan earthquakes, for the purpose of reference, the relation between M_I and M_H for $M_I < 8$ is presented as:

$$M_I = (3.700 \pm 0.512) + (0.409 \pm 0.081)M_H \quad (40)$$

(4) Relation of $M_s(\text{GR})$ vs. m_B

$M_s(\text{GR})$ and m_B are two magnitudes scales used by Gutenberg and Richter to quantify earthquakes before 1954. Their relation for Taiwan earthquakes is in the form:

$$m_B = (0.17 \pm 0.80) + (0.96 \pm 0.11)M_s(\text{GR}) \quad (41)$$

by Wang and Miyamura (1990). This equation is different from that obtained by Gutenberg and Richter (1954):

$$m_B = 2.5 + 0.63M_s(\text{GR}) \quad (42)$$

for global earthquakes.

(5) Relations of M_J vs. $M_s(\text{GR})$ and M_J vs. m_B

The relation between M_J and $M_s(\text{GR})$ is in the form:

$$M_J = (0.25 \pm 0.34) + (0.96 \pm 0.05)M_s(\text{GR}) \quad (43)$$

by Wang and Miyamura (1990). Although the M_s (GR) values were determined by taking the mean of the maximum amplitudes of wave motions from various raypaths worldwide, while the M_J values were determined only from those passing through the region between Taiwan and Japan, high correction of the two regression equations implicates the equality of the two magnitudes for Taiwan earthquakes.

The relation between M_J and m_B is

$$M_J = (-2.68 \pm 1.38) + (1.38 \pm 0.19)m_B \quad (44)$$

by Wang and Miyamura (1990).

(6) Relations of M_o vs. M_s , M_o vs. m_b and M_o vs. M_L

Since the M_o values were not determined for earthquakes which occurred before 1970, there is an attempt to estimate the M_o values for such events through a simple method by the conversion formula between M_o and magnitude. For Taiwan earthquakes, Wang (1985) related M_o to M_s in the form:

$$\log M_o = 1.20M_s + 17.83 \quad (45)$$

and to m_b in the form:

$$\log M_o = 1.90m_b + 14.19 \quad (46)$$

The two regression equations for Taiwan earthquakes agree closely with the average seismic moment-magnitude relations for the Pacific plate margin earthquakes obtained by Nuttli (1983). But the M_s - m_b relation for Taiwan earthquakes is different from that for the Pacific plate margin ones by Nuttli (1983). Seismic moment calculated from very long-period surface waves is associated with static property of the fault; while the M_s determined from surface waves with period of about 20 sec and the m_b determined from body waves with period of about 1 sec are both related to kinematic rupture on the fault. Given results might show the tectonics in the Taiwan region are similar to that in the whole Pacific plate margin but the rupture process of earthquake in the former might be different from the average one in the latter. The relation between M_o and M_L is in the form:

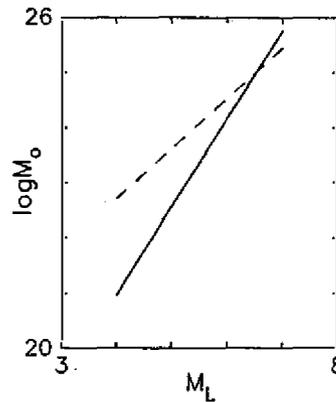
$$\log M_o = (14.571 \pm 1.683) + (1.598 \pm 0.236)M_L \quad (47)$$

by Wang *et al.* (1989). The M_o (LC) determined the formula by Li and Chiu (1989) is related to the M_L in the form:

$$\log M_o(LC) = (19.043 \pm 0.533) + (0.914 \pm 0.035)M_L \quad (48)$$

Eqs. (47) and (48) are shown in Figure 8. It is obvious that the two equations do not agree with each other. The M_o values applied to determine Eq. (47) can be considered as the standard ones because they were estimated from very long-period surface waves. Hence the difference of Eqs. (47) and (48) might show that the M_o (LC) values were overestimated for $M_L < 6.5$ and underestimated for $M_L > 6.5$.

Fig. 8. Figure shows the $\log M_o$ - M_L relations from Li and Chiu (1989) in dashed line and Wang *et al.* (1989) in solid line.



The selection of the "d" value in Eq. (23) is questionable. The optimum value chosen by Bolt and Herraiz (1983) was the time between the S (with amplitude C) onset and the point having an amplitude $c/C=1/3$, while Li and Chiu's result is $c/C=1/2$. A physically reasonable interpretation about the d value is needed before the use of the Bolt and Herraiz's technique (1977) to determine M_o from local seismograms.

4. CONCLUSIONS

From the above discussion, several points can be derived as follows:

1. The M_L - M_D relations obtained by three groups of authors are similar.
2. The three M_L - M_H relations obtained by Yeh and his coauthors are essentially the same.
3. The M_L - m_b relations obtained by Shin (1986) and Wang *et al.* (1989) are close to each other even their data sets are different. But they are remarkably different from that obtained by Cheng and Yeh (1989).
4. The M_D - m_b relations obtained by Shin (1986) and Wang and Chiang (1987) are almost the same.
5. Although the formula to determine the M_H by Hsu (1971) was originally defined based on a Japanese M_s - m_b conversion relation and determined from local seismograms, the correction between M_H and M_s (GR) as well as M_H and M_s for Taiwan earthquakes is good enough. Consequently, although Hsu's magnitude was determined from local seismograms, it is like a surface-wave magnitude in the practical use.
6. The $\log M_o$ - M_L relations obtained by Li and Chiu (1989) and Wang *et al.* (1989) are quite different. For $M_L > 6.65$, $M_o(\text{LC}) < M_o(\text{EDR})$ and for $M_L < 6.65$, $M_o(\text{LC}) > M_o(\text{EDR})$. In other words, $M_o(\text{LC})$ might be overestimated for $M_L < 6.5$ and underestimated for $M_L > 6.5$.

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台灣地震的各種規模及其等間關係式之回顧

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摘要

本文回顧並說明自 1900 年以來用於表示台灣地震大小之各種規模，如 M_L ， M_D ， $M_S(GR)$ ， m_B ， M_S ， m_b ， M_H ， M_J 和 M_I 。同時這些規模間之關係式亦一併在文中討論。